

Shortest Counterexamples for Symbolic Model Checking of LTL with Past

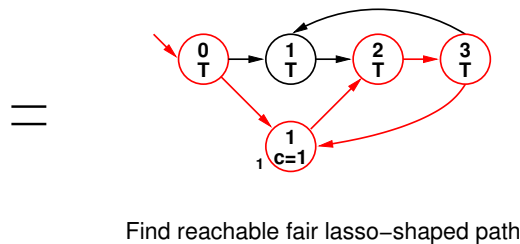
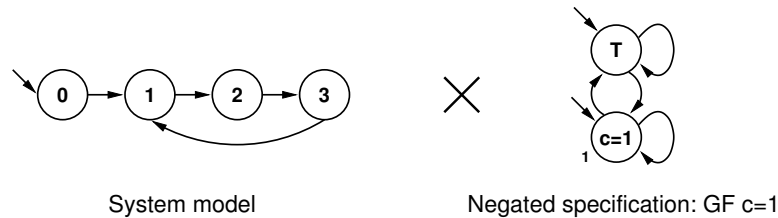
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To obtain **shortest counterexample**

1. Find **shortest** fair lasso-shaped path.

SAT-based BMC [Biere, Cimatti, Clarke, Zhu (TACAS'99)]

BDD-based symbolic MC [Schuppan, Biere (STTT'04)]

explicit-state MC [Gastin, Moro, Zeitoun (SPIN'04)]

2. Have **tight** automaton/encoding of specification.

SAT-based BMC [Benedetti, Cimatti (TACAS'03)]

[Latvala, Biere, Heljanko, Junttila (VMCAI'05)]

BDD-based symbolic MC **this talk**

explicit-state MC **(this talk)**

1. Introduction
2. Preliminaries
3. Criteria for Tight Büchi Automata
4. Tight Büchi Automaton for LTL with Past
5. Experimental Results
6. Conclusion

Shortest Infinite Counterexamples

[Clarke, Grumberg, McMillan, Zhao (DAC'95)]

Finite state system with failing LTL property:

\Rightarrow **lasso-shaped** counterexample $\alpha = \beta\gamma^\omega$

$$\alpha = \underbrace{b_0 b_1 b_2 \dots b_{|\beta|-1}}_{\text{stem } \beta} \underbrace{c_0 c_1 c_2 \dots c_{|\gamma|-1}}_{\text{loop } \gamma} \underbrace{c_0 c_1 c_2 \dots c_{|\gamma|-1} \dots}_{\text{loop body } \gamma^\omega}$$

length of counterexample: $|\text{stem } \beta| + |\text{loop } \gamma|$

Shortest infinite counterexample \Rightarrow **minimal** $|\beta| + |\gamma|$.

[Kupferman, Vardi (CAV'99)]:

Automaton on **finite words** tight

\Leftrightarrow

accepts shortest violating prefixes for safety properties.

Extend notion:

Büchi automaton on **infinite words** tight

\Leftrightarrow

for each lasso-shaped counterexample α there is a fair, lasso-shaped path in the product with α of the same length.

Formally:

$$\begin{aligned} &\forall \alpha \in \text{Lang}(B) . \forall \beta, \gamma . (\alpha = \beta\gamma^\omega \Rightarrow \\ &\quad \exists \rho \in \text{Runs}(B) . \exists \lambda, \mu, \nu . \\ &\quad (\rho \models \alpha \wedge \lambda = \alpha \times \rho = \mu\nu^\omega \wedge |\mu| + |\nu| = |\beta| + |\gamma|)) \end{aligned}$$

Specification: $\neg(\mathbf{GF}(c = 1) \wedge \mathbf{GF}(c = 3))$

Automaton	Path
	$(0) \quad (1 \ 2 \ 3 \ 2) \quad (1 \ 2 \ 3 \ 2) \quad (1 \ 2 \ 3 \ 2) \quad \dots$
×	×
?	$(r_0) \quad (r_1 \ r_2 \ r_3 \ r_4) \quad (r_1 \ r_2 \ r_3 \ r_4) \quad (r_1 \ r_2 \ r_3 \ r_4) \quad \dots$
=	=
?	$\begin{pmatrix} 0 \\ r_0 \end{pmatrix} \begin{pmatrix} 1 & 2 & 3 & 2 \\ r_1 & r_2 & r_3 & r_4 \end{pmatrix} \begin{pmatrix} 1 & 2 & 3 & 2 \\ r_1 & r_2 & r_3 & r_4 \end{pmatrix} \begin{pmatrix} 1 & 2 & 3 & 2 \\ r_1 & r_2 & r_3 & r_4 \end{pmatrix} \dots$

What do system states of the **same color** have in common?

⇒ They have the **same future**. (But different past.)

Specification: $\neg(\mathbf{GF}(c = 1) \wedge \mathbf{GF}(c = 3))$

Automaton	Path
	$(0) \quad (1 \ 2 \ 3 \ 2) \quad (1 \ 2 \ 3 \ 2) \quad (1 \ 2 \ 3 \ 2) \quad \dots$
\times	\times
$?$	$(r_0) \quad (r_1 \ r_2 \ r_3 \ r_4) \quad (r_1 \ r_2 \ r_3 \ r_4) \quad (r_1 \ r_2 \ r_3 \ r_4) \quad \dots$
$=$	$=$
$?$	$\begin{pmatrix} 0 \\ r_0 \end{pmatrix} \begin{pmatrix} 1 & 2 & 3 & 2 \\ r_1 & r_2 & r_3 & r_4 \end{pmatrix} \begin{pmatrix} 1 & 2 & 3 & 2 \\ r_1 & r_2 & r_3 & r_4 \end{pmatrix} \begin{pmatrix} 1 & 2 & 3 & 2 \\ r_1 & r_2 & r_3 & r_4 \end{pmatrix} \dots$

Büchi automaton must have accepting run that pairs system states with **same future** with **same state**.

(Non-) Tightness of Tableau

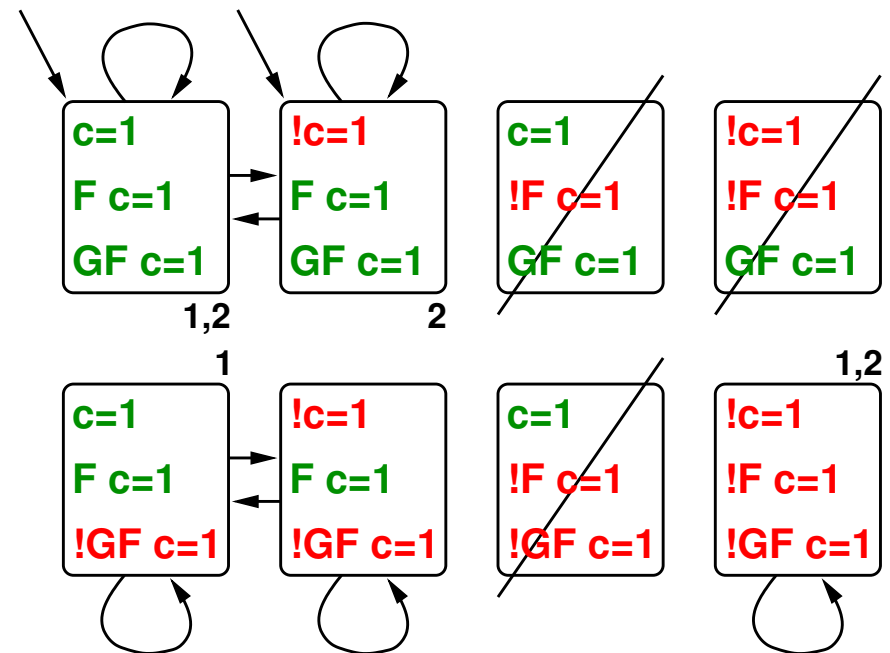
Tableau following [Kesten, Pnueli, Raviv (ICALP'98)]

- State bits represent subformulae of ϕ .
- If ρ is accepting run on α : formulae in $\rho(i)$ hold at $\alpha(i)$.
- Each pair of states differs in sign of ≥ 1 formulae:
 \Rightarrow different future and/or past.

Tableau is

- \Rightarrow tight for future time LTL.
- \Rightarrow not tight for LTL with past.

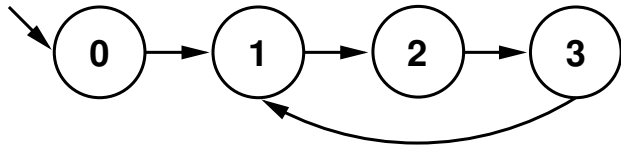
Tableau for $\phi = \mathbf{GF}(c = 1)$



Problem with Past Time Formulae

simplified from [Benedetti, Cimatti '03]

System model



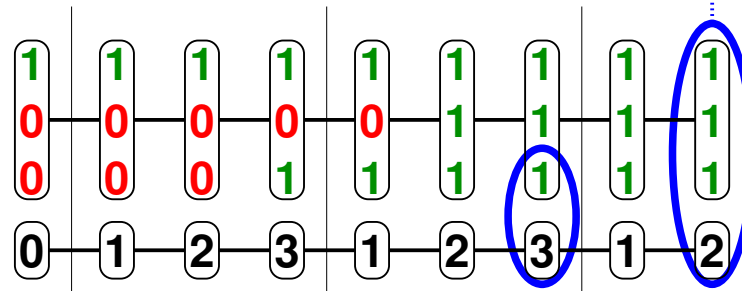
Specification

$$\neg \mathbf{F}(\mathbf{O}((c = 2) \wedge \mathbf{O}(c = 3)))$$

Shortest counterexample has length 4.

Accepting lasso in tableau

$\mathbf{F}(\mathbf{O}((c=2) \ \& \ \mathbf{O}(c=3)))$
 $\mathbf{O}((c=2) \ \& \ \mathbf{O}(c=3))$
 $\mathbf{O}(c=3)$
 c



close loop for c and all subformulae

close loop for c and O(c=3)

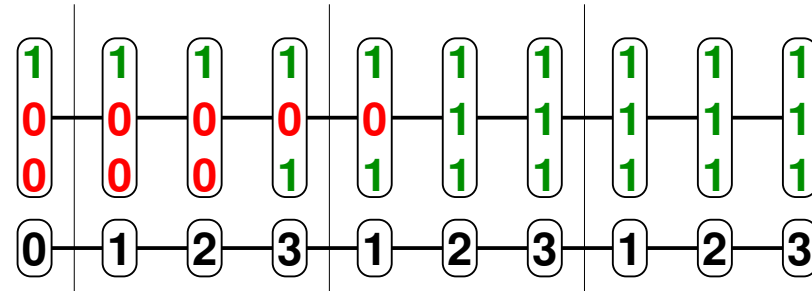
Accepting lasso has length 8.

$F(O((c=2) \ \& \ O(c=3)))$

$O((c=2) \ \& \ O(c=3))$

$O(c=3)$

c



[Laroussinie, Markey, Schnoebelen (LICS'02)], [Benedetti, Cimatti '03]:

- Let $h(\phi)$ be the maximal number of nested past time operators (past operator depth)
- Truth of past time formula ϕ “stable” after $h(\phi) + 1$ loop iterations

Hence:

The length of a shortest counterexample generated by the tableau construction is bounded by $O(l \cdot h(\phi))$.

(l : length of shortest counterexample)

Same problem faced by bounded model checking of LTL with past

Solution: virtual unrolling of transition relation

[Benedetti, Cimatti '03], [Latvala et al. '05]

⇒ Encoding of Latvala et al. can be transformed into Büchi automaton

⇒ Give automata-oriented perspective on virtual unrolling

(some similarity with [history transducer](#)

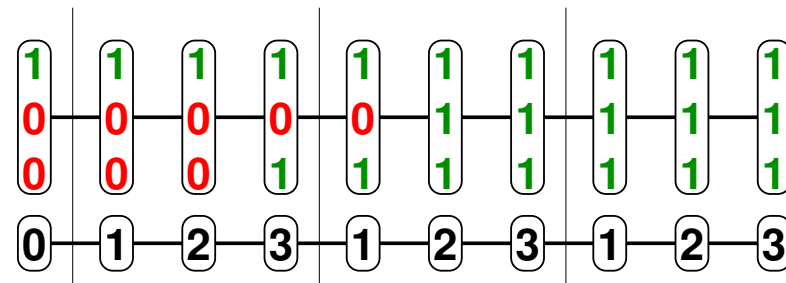
by [Jonsson, Nilsson (TACAS'00)])

$F(O((c=2) \ \& \ O(c=3)))$

$O((c=2) \ \& \ O(c=3))$

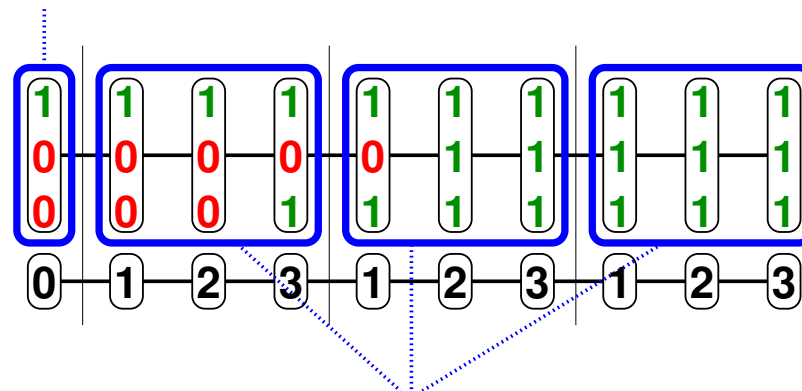
$O(c=3)$

c



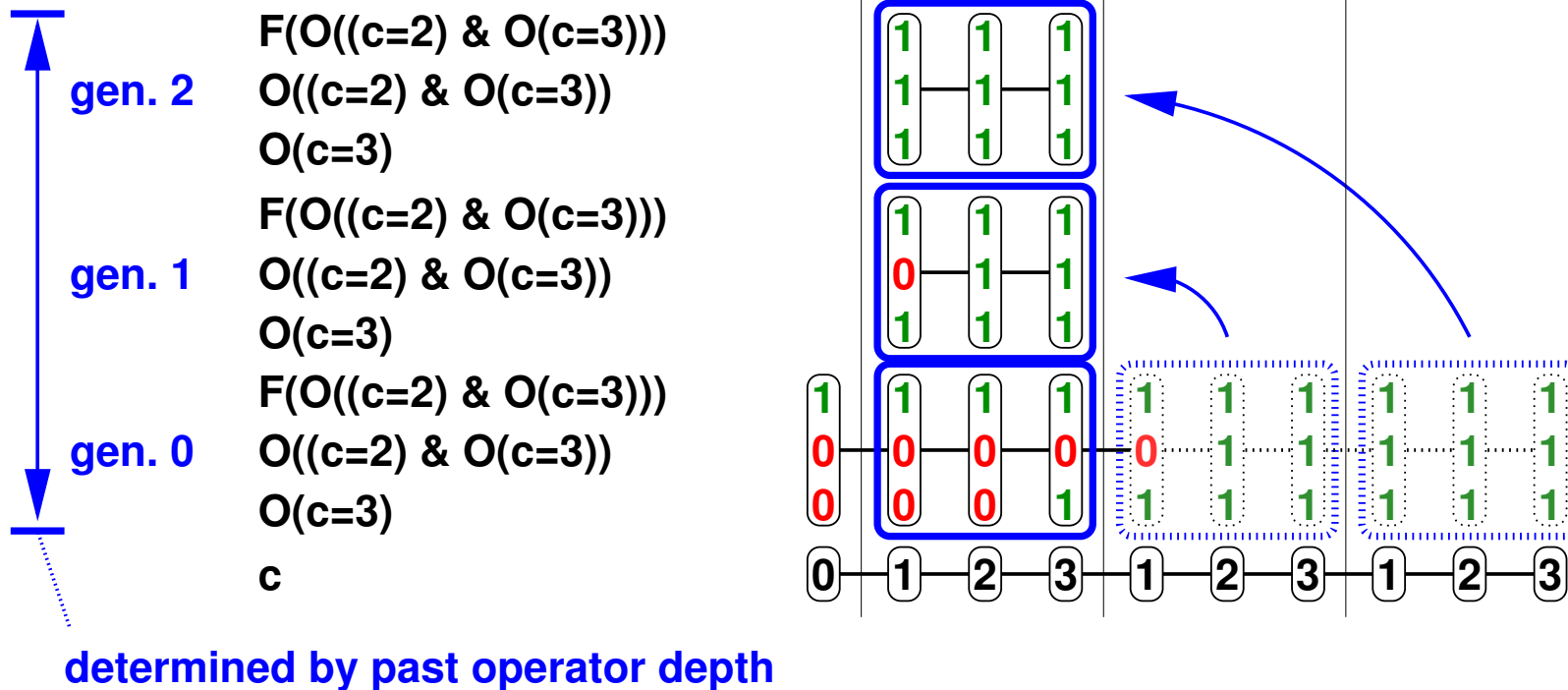
no need to change

$F(O((c=2) \ \& \ O(c=3)))$
 $O((c=2) \ \& \ O(c=3))$
 $O(c=3)$
 c



these work on the same subsequence
of the counterexample...

have states of old automaton work in parallel:
introduce several generations of variables

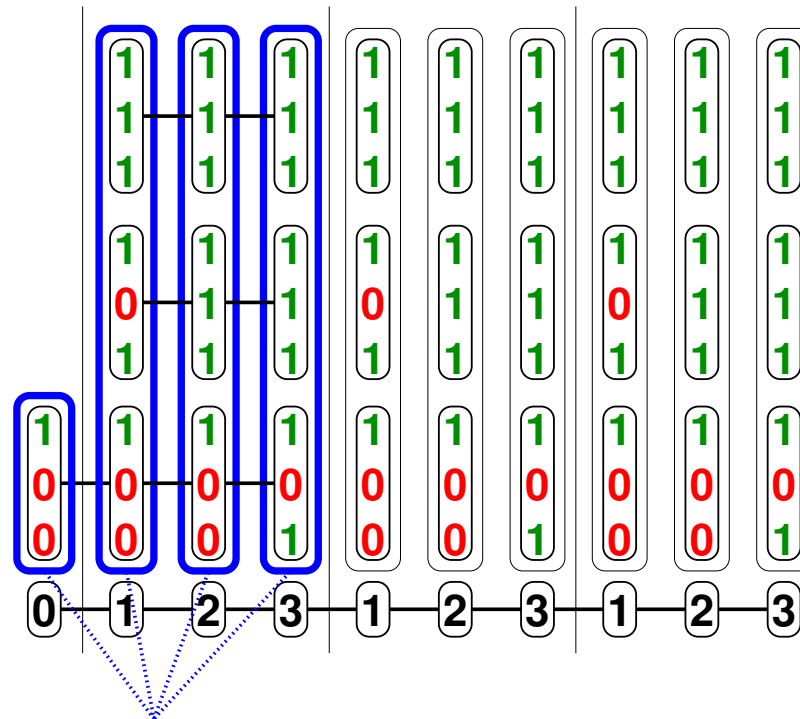


gen. 2 $F(O((c=2) \ \& \ O(c=3)))$
 $O((c=2) \ \& \ O(c=3))$
 $O(c=3)$

gen. 1 $F(O((c=2) \ \& \ O(c=3)))$
 $O((c=2) \ \& \ O(c=3))$
 $O(c=3)$

gen. 0 $F(O((c=2) \ \& \ O(c=3)))$
 $O((c=2) \ \& \ O(c=3))$
 $O(c=3)$

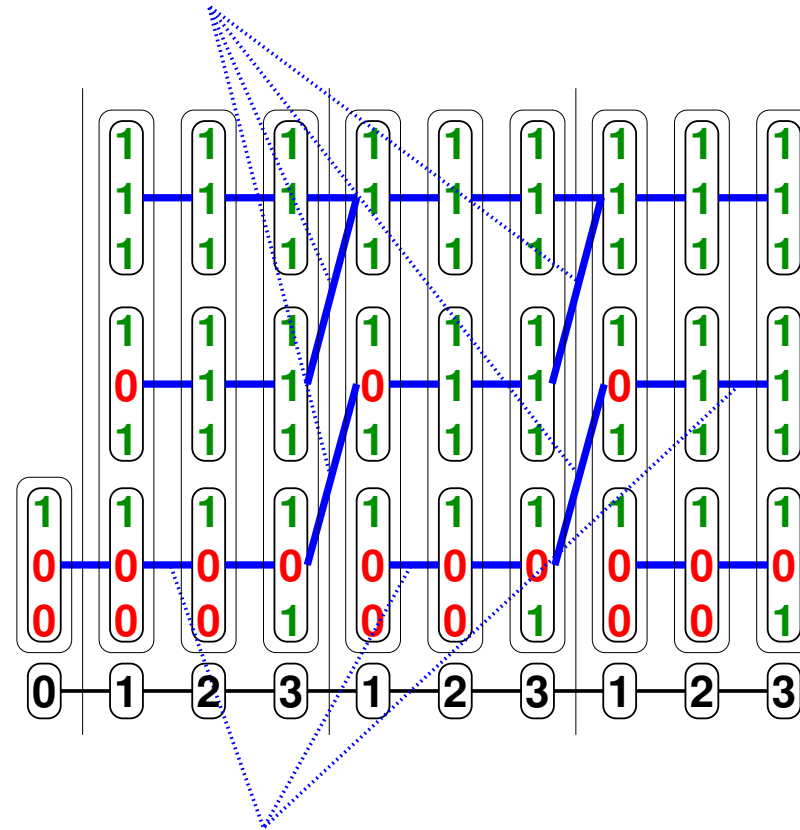
c



"tuple" states of new automaton

at end of iteration:
constraints between subsequent generations

gen. 2 $F(O((c=2) \ \& \ O(c=3)))$
 $O((c=2) \ \& \ O(c=3))$
 $O(c=3)$
 gen. 1 $F(O((c=2) \ \& \ O(c=3)))$
 $O((c=2) \ \& \ O(c=3))$
 $O(c=3)$
 gen. 0 $F(O((c=2) \ \& \ O(c=3)))$
 $O((c=2) \ \& \ O(c=3))$
 $O(c=3)$
 c



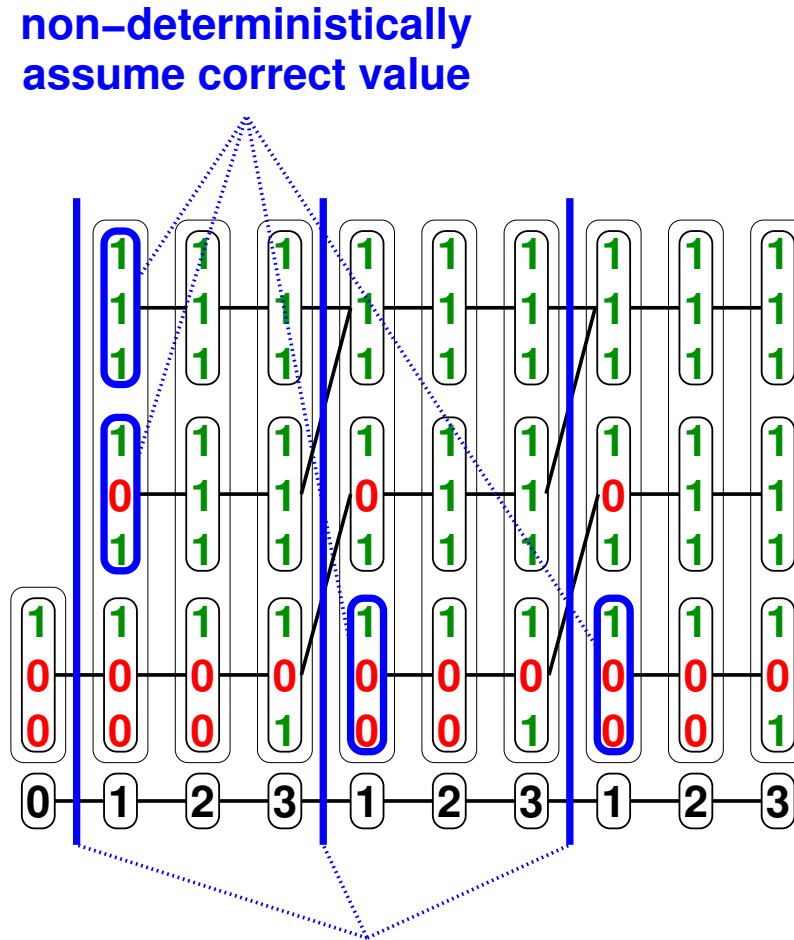
within iteration:
constraints between same generation

gen. 2 $F(O((c=2) \ \& \ O(c=3)))$
 $O((c=2) \ \& \ O(c=3))$
 $O(c=3)$

gen. 1 $F(O((c=2) \ \& \ O(c=3)))$
 $O((c=2) \ \& \ O(c=3))$
 $O(c=3)$

gen. 0 $F(O((c=2) \ \& \ O(c=3)))$
 $O((c=2) \ \& \ O(c=3))$
 $O(c=3)$

c



non-deterministic detection of
loop body and end of iteration

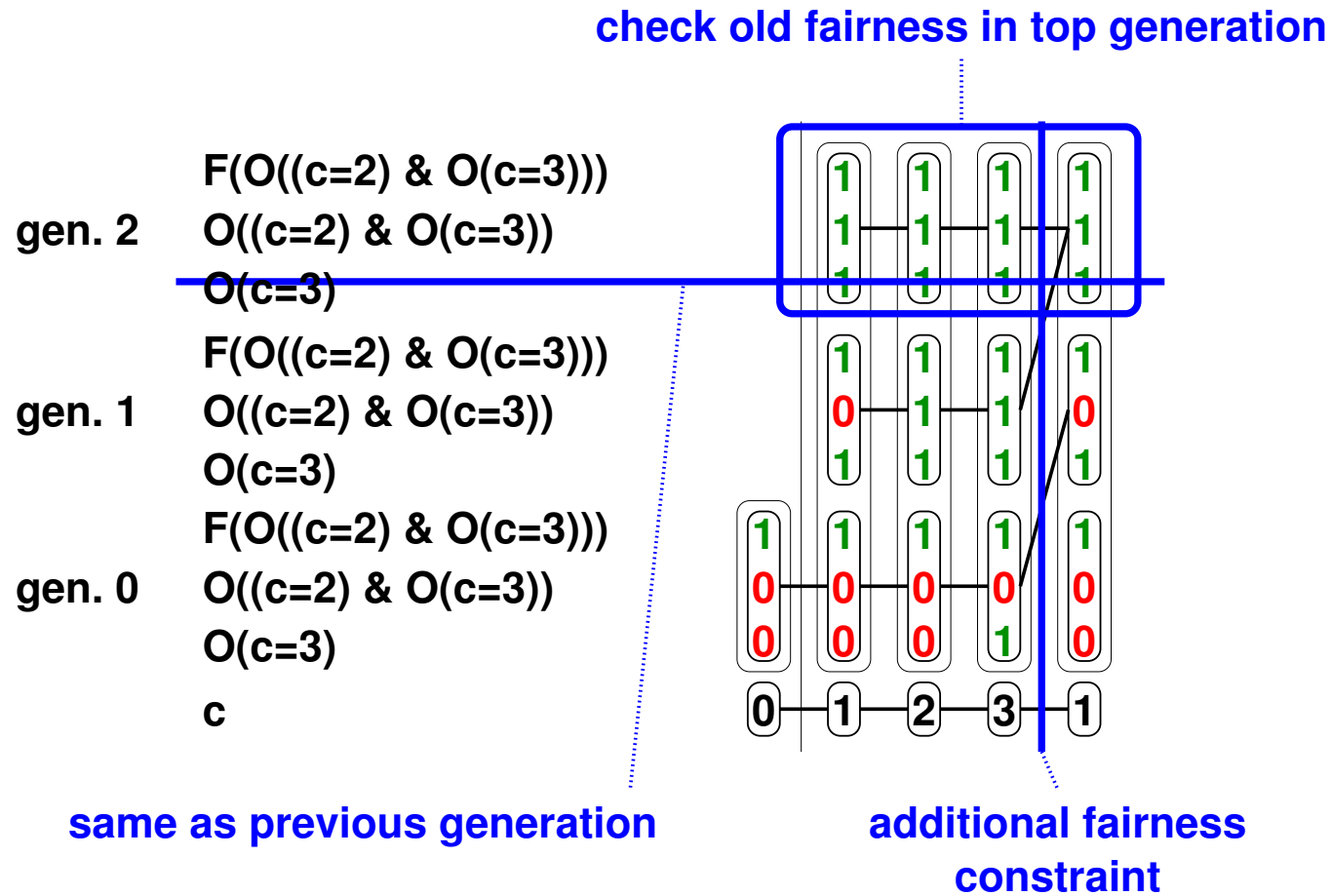


	Tableau	Tight Tableau
$V\Psi$	$V\Psi_1 \cup \{x_\Psi\}$	$V\Psi_1 \cup \bigcup_{i=0}^{h(\Psi)} \{x_{\Psi,i}\}$
$T\Psi$	$T\Psi_1$ $\wedge (x'_\Psi \leftrightarrow x'_{\Psi_1} \vee x_\Psi)$	$T\Psi_1$ $\wedge (\neg lb \rightarrow (x'_{\Psi,0} \leftrightarrow x'_{\Psi_1,0} \vee x_{\Psi,0}))$ $\wedge ((lb \wedge \neg le) \rightarrow \bigwedge_{i=0}^{h(\Psi)-1} (x'_{\Psi,i} \leftrightarrow x'_{\Psi_1,i} \vee x_{\Psi,i}))$ $\wedge ((lb \wedge le) \rightarrow \bigwedge_{i=0}^{h(\Psi)-2} (x'_{\Psi,i+1} \leftrightarrow x'_{\Psi_1,i+1} \vee x_{\Psi,i}))$ $\wedge (lb \rightarrow (x'_{\Psi,h(\Psi)} \leftrightarrow x'_{\Psi_1,h(\Psi_1)} \vee x_{\Psi,h(\Psi)}))$
$I\Psi$	$I\Psi_1 \wedge (x_\Psi \leftrightarrow x_{\Psi_1})$	$I\Psi_1 \wedge (x_{\Psi,0} \leftrightarrow x_{\Psi_1,0})$
$F\Psi$	$F\Psi_1$	$F\Psi_1$

lb is true on the loop body

le is true at the end of a loop iteration

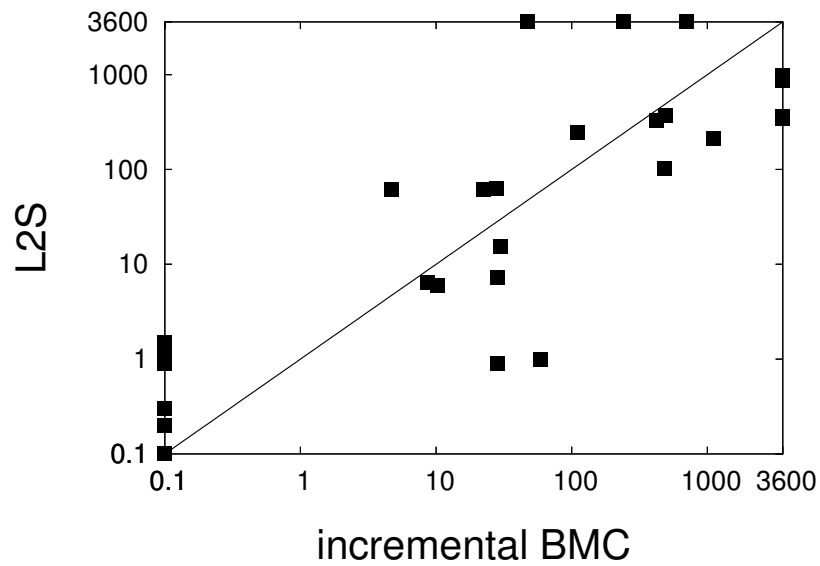
Compare finding shortest counterexamples with tight tableau

- SAT-based BMC [Heljanko, Junttila, Latvala, CAV'05]
⇒ **preliminary** incremental implementation of [Latvala et al. '05]
(modified NuSMV 2.2.2, marked **incremental BMC**)
- BDD-based symbolic loop detection [Schuppan, Biere '04]
(on top of NuSMV 2.2.2, marked **L2S**)

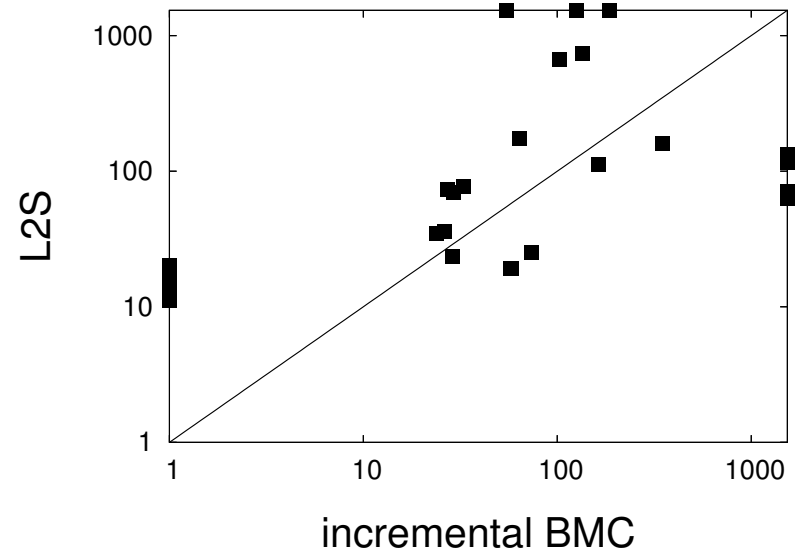
Remarks

- No cone of influence reduction
- For BDDs: no dynamic reordering
- For BMC: choice of 2 SAT solvers: zchaff, minisat
⇒ use minimum time/memory
- Examples (all false, resulting in counterexample):
 - [Latvala et al. '05] (some slightly changed)
 - [Schuppan, Biere '04] (some additional properties)

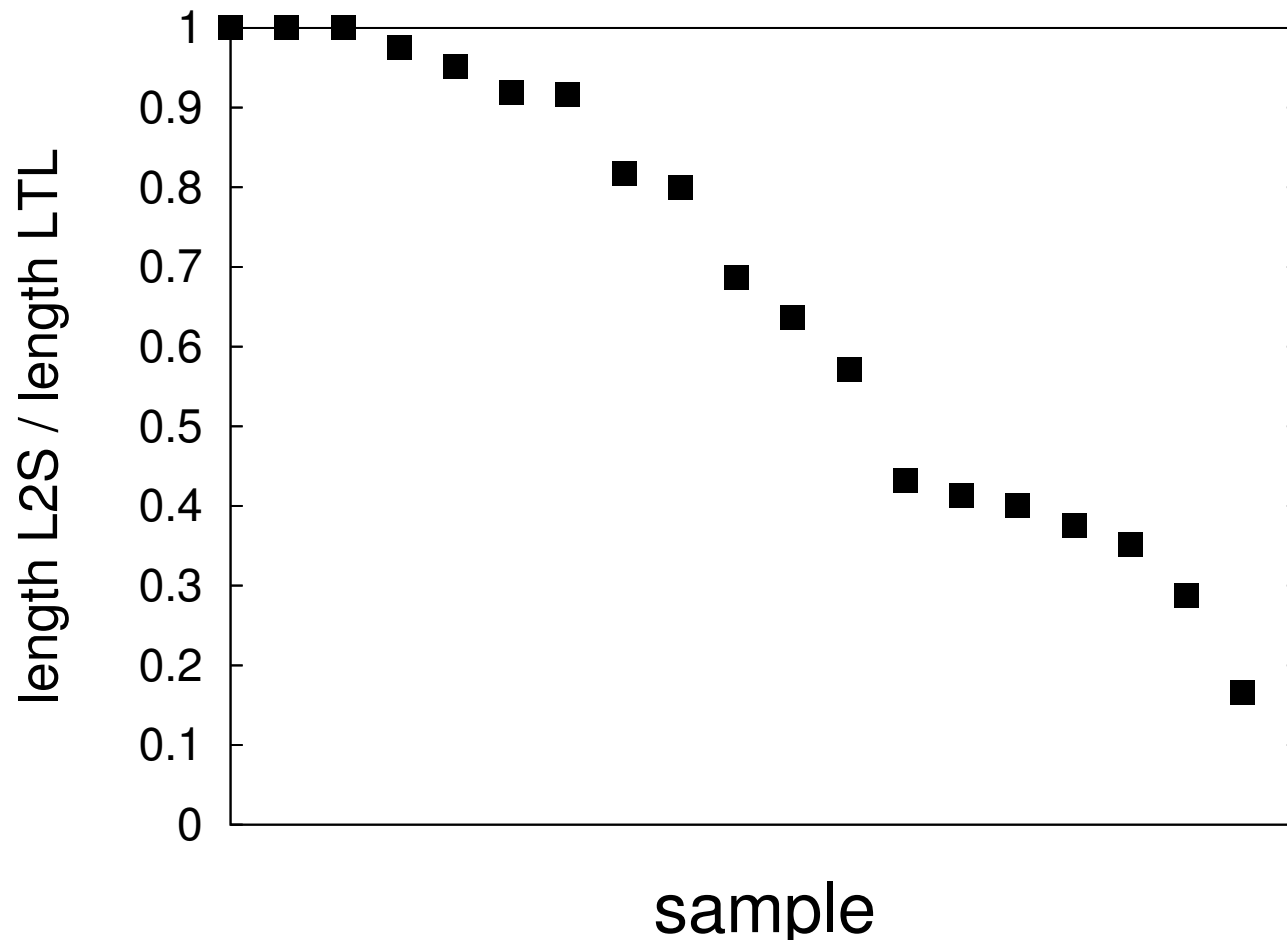
L2S vs incremental BMC
– CPU time [sec]



L2S vs incremental BMC
– Memory [MB]



L2S versus LTL – length counterexample



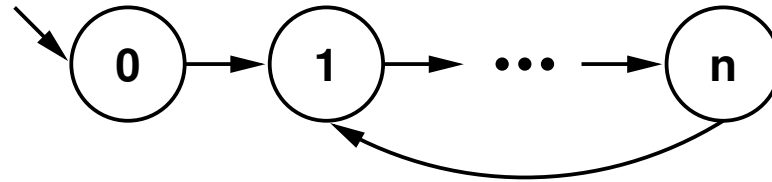
Summary

- Criteria for Büchi automata to accept shortest counterexamples
- Prove tableau [Kesten et al. '98] tight for future time LTL, not tight for LTL with past
- Practical method to find shortest counterexamples with BDD-based symbolic model checker
 - ⇒ runtime competitive with bounded model checking

Future work

- Explicit-state model checking (size, on-the-fly)
- Lower bounds

Keep out!
Backup slides



$$\neg \mathbf{G}((c \neq n) \quad \mathbf{U}((c = n) \quad \wedge \\ ((c \neq n - 1) \mathbf{U}((c = n - 1) \wedge \\ \dots \\ ((c \neq 1) \quad \mathbf{U}(c = 1)) \\ \dots \\))))$$

automaton of [Gerth, Peled, Vardi, Wolper (PSTV'95)]:
counterexample of length $\mathbf{O}(n^2)$.

$$\neg(\mathbf{F}(\mathbf{G}(\mathbf{O}((c = 1) \wedge \\ \mathbf{O}((c = 2) \wedge \\ \dots \\ \mathbf{O}(c = n) \\ \dots \\)))))$$

automaton of [Kesten, Pnueli, Raviv (ICALP'98)]:
counterexample of length $\mathbf{O}(n^2)$.

Shortest counterexample has length $n + 1$.

The following are equivalent:

1. $\forall \alpha \in \text{Lang}(B) . \forall \beta, \gamma . (\alpha = \beta\gamma^\omega \Rightarrow \exists \rho \in \text{Runs}(B) . \exists \lambda, \mu, \nu . (\rho \models \alpha \wedge \lambda = \alpha \times \rho = \mu\nu^\omega \wedge |\mu| + |\nu| = |\beta| + |\gamma|))$
2. $\forall \alpha \in \text{Lang}(B) . \forall \beta, \gamma . ((\alpha = \beta\gamma^\omega \wedge |\beta| + |\gamma| \text{ minimal for } \alpha) \Rightarrow \exists \rho \in \text{Runs}(B) . \exists \lambda, \mu, \nu . (\rho \models \alpha \wedge \lambda = \alpha \times \rho = \mu\nu^\omega \wedge |\mu| + |\nu| = |\beta| + |\gamma|))$
3. $\forall \alpha \in \text{Lang}(B) . ((\exists \beta, \gamma . \alpha = \beta\gamma^\omega) \Rightarrow (\exists \rho \in \text{Runs}(B) . (\rho \models \alpha \wedge (\forall i, j . \alpha[i, \infty] = \alpha[j, \infty] \Rightarrow \rho(i) = \rho(j))))))$
4. $\forall \alpha \in \text{Lang}(B) . \forall \beta, \gamma . ((\alpha = \beta\gamma^\omega \wedge |\beta| + |\gamma| \text{ minimal for } \alpha) \Rightarrow \exists \rho \in \text{Runs}(B) . \exists \sigma, \tau . (\rho \models \alpha \wedge \rho = \sigma\tau^\omega \wedge |\sigma| = |\beta| \wedge |\tau| = |\gamma|))$
5. $\forall \alpha \in \text{Lang}(B) . \forall \beta, \gamma . (\alpha = \beta\gamma^\omega \Rightarrow \exists \rho \in \text{Runs}(B) . \exists \sigma, \tau . (\rho \models \alpha \wedge \rho = \sigma\tau^\omega \wedge |\sigma| = |\beta| \wedge |\tau| = |\gamma|))$

	Tableau	Tight Tableau
V_{BA}^ϕ	V^ϕ	$V^\phi \cup \{lb, le\}$
T_{BA}^ϕ	T^ϕ	$T^\phi \wedge lb \rightarrow lb'$
I_{BA}^ϕ	$I^\phi \wedge x_\phi$	$I^\phi \wedge x_{\phi,0}$
F_{BA}^ϕ	F^ϕ	$F^\phi \cup \{\{lb \wedge le\}\}$

$V^\phi, T^\phi, I^\phi, F^\phi$ are defined recursively on the following slides.

	Tableau	Tight Tableau
V^ψ	$V^{\psi_1} \cup \{x_\psi\}$	$V^{\psi_1} \cup \bigcup_{i=0}^{h(\psi)} \{x_{\psi,i}\}$
T^ψ	$T^{\psi_1} \wedge (x_\psi \leftrightarrow x'_{\psi_1})$	T^{ψ_1} $\wedge (\neg lb \rightarrow (x_{\psi,0} \leftrightarrow x'_{\psi_1,0}))$ $\wedge ((lb \wedge \neg le) \rightarrow \bigwedge_{i=0}^{h(\psi)-1} (x_{\psi,i} \leftrightarrow x'_{\psi_1,i}))$ $\wedge ((lb \wedge le) \rightarrow \bigwedge_{i=0}^{h(\psi)-1} (x_{\psi,i} \leftrightarrow x'_{\psi_1,i+1}))$ $\wedge (lb \rightarrow (x_{\psi,h(\psi)} \leftrightarrow x'_{\psi_1,h(\psi_1)}))$
I^ψ	I^{ψ_1}	I^{ψ_1}
F^ψ	F^{ψ_1}	F^{ψ_1}

	Tableau	Tight Tableau
V^Ψ	$V^{\psi_1} \cup V^{\psi_2} \cup \{x_\psi\}$	$V^{\psi_1} \cup V^{\psi_2} \cup \bigcup_{i=0}^{h(\psi)} \{x_{\psi,i}\}$
T^Ψ	$T^{\psi_1} \wedge T^{\psi_2}$ $\wedge (x_\psi \leftrightarrow x_{\psi_2} \vee x_{\psi_1} \wedge x'_\psi)$	$T^{\psi_1} \wedge T^{\psi_2}$ $\wedge (\neg lb \rightarrow (x_{\psi,0} \leftrightarrow x_{\psi_2,0} \vee (x_{\psi_1,0} \wedge x'_{\psi,0})))$ $\wedge ((lb \wedge \neg le) \rightarrow \bigwedge_{i=0}^{h(\psi)-1} (x_{\psi,i} \leftrightarrow x_{\psi_2, \min(i, h(\psi_2))} \vee (x_{\psi_1, \min(i, h(\psi_1))} \wedge x'_{\psi,i})))$ $\wedge ((lb \wedge le) \rightarrow \bigwedge_{i=0}^{h(\psi)-1} (x_{\psi,i} \leftrightarrow x_{\psi_2, \min(i, h(\psi_2))} \vee (x_{\psi_1, \min(i, h(\psi_1))} \wedge x'_{\psi, i+1})))$ $\wedge (lb \rightarrow (x_{\psi, h(\psi)} \leftrightarrow x_{\psi_2, h(\psi_2)} \vee (x_{\psi_1, h(\psi_1)} \wedge x'_{\psi, h(\psi)})))$
I^Ψ	$I^{\psi_1} \wedge I^{\psi_2}$	$I^{\psi_1} \wedge I^{\psi_2}$
F^Ψ	$F^{\psi_1} \cup F^{\psi_2}$ $\cup \{\{\neg x_\psi \vee x_{\psi_2}\}\}$	$F^{\psi_1} \cup F^{\psi_2} \cup \{\{\neg x_{\psi, h(\psi)} \vee x_{\psi_2, h(\psi_2)}\}\}$

	Tableau	Tight Tableau
V^Ψ	$V^{\Psi_1} \cup \{x_\Psi\}$	$V^{\Psi_1} \cup \bigcup_{i=0}^{h(\Psi)} \{x_{\Psi,i}\}$
T^Ψ	$T^{\Psi_1} \wedge (x'_\Psi \leftrightarrow x_{\Psi_1})$	T^{Ψ_1} $\wedge (\neg lb \rightarrow (x'_{\Psi,0} \leftrightarrow x_{\Psi_1,0}))$ $\wedge ((lb \wedge \neg le) \rightarrow \bigwedge_{i=0}^{h(\Psi)-1} (x'_{\Psi,i} \leftrightarrow x_{\Psi_1,i}))$ $\wedge ((lb \wedge le) \rightarrow \bigwedge_{i=0}^{h(\Psi)-2} (x'_{\Psi,i+1} \leftrightarrow x_{\Psi_1,i}))$ $\wedge (lb \rightarrow (x'_{\Psi,h(\Psi)} \leftrightarrow x_{\Psi_1,h(\Psi_1)}))$
I^Ψ	$I^{\Psi_1} \wedge (x_\Psi \leftrightarrow \perp)$	$I^{\Psi_1} \wedge (x_{\Psi,0} \leftrightarrow \perp)$
F^Ψ	F^{Ψ_1}	F^{Ψ_1}

	Tableau	Tight Tableau
V^Ψ	$V^{\Psi_1} \cup V^{\Psi_2} \cup \{x_\Psi\}$	$V^{\Psi_1} \cup V^{\Psi_2} \cup \bigcup_{i=0}^{h(\Psi)} \{x_{\Psi,i}\}$
T^Ψ	$T^{\Psi_1} \wedge T^{\Psi_2}$ $\wedge (x'_\Psi \leftrightarrow x'_{\Psi_2} \vee x'_{\Psi_1} \wedge x_\Psi)$	$T^{\Psi_1} \wedge T^{\Psi_2}$ $\wedge (\neg lb \rightarrow (x'_{\Psi,0} \leftrightarrow x'_{\Psi_2,0} \vee (x'_{\Psi_1,0} \wedge x_{\Psi,0})))$ $\wedge ((lb \wedge \neg le) \rightarrow \bigwedge_{i=0}^{h(\Psi)-1} (x'_{\Psi,i} \leftrightarrow x'_{\Psi_2, \min(i, h(\Psi_2))} \vee (x'_{\Psi_1, \min(i, h(\Psi_1))} \wedge x_{\Psi,i})))$ $\wedge ((lb \wedge le) \rightarrow \bigwedge_{i=0}^{h(\Psi)-1} (x'_{\Psi, i+1} \leftrightarrow x'_{\Psi_2, \min(i+1, h(\Psi_2))} \vee (x'_{\Psi_1, \min(i+1, h(\Psi_1))} \wedge x_{\Psi,i})))$ $\wedge (lb \rightarrow (x'_{\Psi, h(\Psi)} \leftrightarrow x'_{\Psi_2, h(\Psi_2)} \vee (x'_{\Psi_1, h(\Psi_1)} \wedge x_{\Psi, h(\Psi)})))$
I^Ψ	$I^{\Psi_1} \wedge I^{\Psi_2} \wedge (x_\Psi \leftrightarrow x_{\Psi_2})$	$I^{\Psi_1} \wedge I^{\Psi_2} \wedge (x_{\Psi,0} \leftrightarrow x_{\Psi_2,0})$
F^Ψ	$F^{\Psi_1} \cup F^{\Psi_2}$	$F^{\Psi_1} \cup F^{\Psi_2}$

Preliminary Exp.s w/ Incremental BMC — Raw Data

		L2S		BMC			
				zchaff		minisat	
model	spec	time [sec]	mem [MB]	time [sec]	mem [MB]	time [sec]	mem [MB]
1394-3-2	0	6.5	34.9	9.8	34.1	8.7	23.9
	1	5.9	35.9	11.3	35.7	10.2	26.2
1394-4-2	0	382.3	665.9	430.6	122.4	423.4	102.6
	1	366.8	742.6	527.2	199.2	493.4	134.8
abp4	L	7.3	23.6	30.2	30.4	28.6	28.8
brp	¬ L	0.3	13.5	0.1	1.0	0.1	1.0
	¬ L, nv	102.5	112.9	486.5	163.2	t.o.	t.o.
dme2	L	1.0	19.3	58.7	58.1	484.4	119.2
	¬ L	0.2	11.4	0.1	1.0	0.1	1.0
	¬ L, nv	0.9	19.3	28.2	57.4	355.2	102.5
dme5	L	348.7	71.0	t.o.	t.o.	t.o.	t.o.
	¬ L	1.0	17.3	0.1	1.0	0.1	1.0
	¬ L, nv	360.8	63.2	t.o.	t.o.	t.o.	t.o.
dme6	L	983.6	133.4	t.o.	t.o.	t.o.	t.o.
	¬ L	1.5	18.3	0.1	1.0	0.1	1.0
	¬ L, nv	866.8	115.5	t.o.	t.o.	t.o.	t.o.
pci	L	m.o.	m.o.	47.5	54.6	104.5	72.8
	F L	m.o.	m.o.	701.6	126.2	2480.2	478.8
	¬ L	0.9	17.1	0.1	13.8	0.1	1.0
prod-cons	0	243.4	175.7	109.7	63.8	299.9	158.2
	1	61.1	69.6	22.2	33.6	25.1	29.2
	2	61.8	73.8	4.7	27.1	103.7	53.5
	3	63.0	77.3	27.9	32.7	25.6	29.4
production-cell	0	15.5	25.0	30.0	73.5	511.1	111.2
	1	t.o.	t.o.	241.8	187.0	559.9	130.4
bc57-sensors	0	211.2	159.6	1112.8	349.2	2306.6	300.1
srg5	¬ L	0.1	11.2	0.1	1.0	0.1	1.0
	¬ L, nv	1.2	20.0	0.1	1.0	0.1	1.0

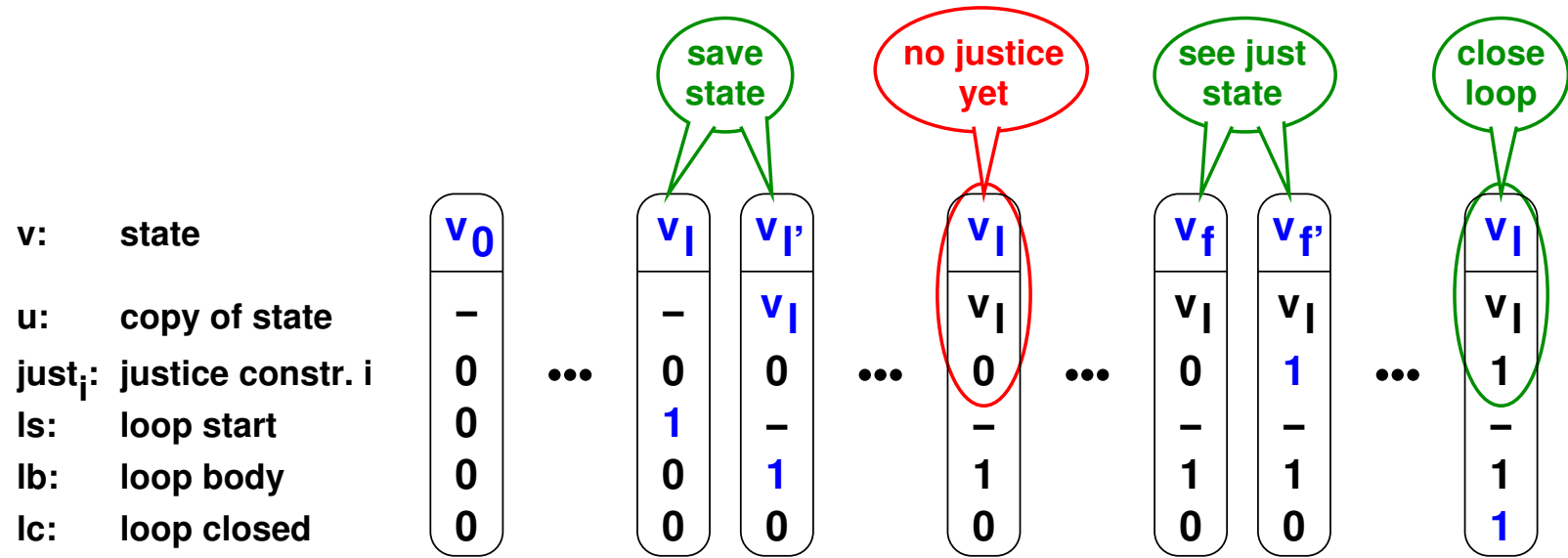
red: best overall blue: best BMC

model	prop	template
1394-3/4-2	0 1	$\neg((\mathbf{F}(\mathbf{G}(p))) \rightarrow (\neg((q) \mathbf{S}(r))))$ $\neg(\mathbf{F}((p) (q (r))))$
abp4	L	$\mathbf{G}((p) \rightarrow (Y(H(q))))$
brp	$\neg L$ $\neg L, nv$	$\neg(\mathbf{F}(\mathbf{G}((p) \rightarrow (\mathbf{O}((q) \rightarrow (\mathbf{O}(r)))))))$ $\neg((\mathbf{F}(\mathbf{G}((p) \rightarrow (\mathbf{O}((q) \rightarrow (\mathbf{O}(r))))))) \wedge ((\mathbf{G}(\mathbf{F}(p))) \wedge (\mathbf{G}(\mathbf{F}(q))))))$
dme2/5/6	(L) $\neg L$ $\neg L, nv$	$\mathbf{G}((p) \rightarrow ((p) \mathbf{T}((\neg(p)) \mathbf{T}(\neg(q))))$ $\neg \mathbf{G}((p) \rightarrow ((p) \mathbf{T}((\neg(p)) \mathbf{T}(\neg(q))))$ $\neg((\mathbf{G}((p) \rightarrow ((p) \mathbf{T}((\neg(p)) \mathbf{T}(\neg(q)))))) \wedge (\mathbf{G}(\mathbf{F}(p))))$
pci	(L) F L ($\neg L$)	$\mathbf{G}((p) \rightarrow (\mathbf{G}(((q) \wedge (\mathbf{Y}(r) \wedge (\mathbf{O}(s) \wedge (\mathbf{O}(t) \wedge (\mathbf{O}(u)))))))) \rightarrow$ $(\mathbf{O}(v) \wedge (\mathbf{O}(w) \wedge (\neg(\mathbf{O}(x))))))))$ $\mathbf{F}(\mathbf{G}((p) \rightarrow (\mathbf{G}(((q) \wedge (\mathbf{Y}(r) \wedge (\mathbf{O}(s) \wedge (\mathbf{O}(t) \wedge (\mathbf{O}(u)))))))) \rightarrow$ $(\mathbf{O}(v) \wedge (\mathbf{O}(w) \wedge (\neg(\mathbf{O}(x))))))))$ $\neg(\mathbf{G}((p) \rightarrow (\mathbf{G}(((q) \wedge (\mathbf{Y}(r) \wedge (\mathbf{O}(s) \wedge (\mathbf{O}(t) \wedge (\mathbf{O}(u)))))))) \rightarrow$ $(\mathbf{O}(v) \wedge (\mathbf{O}(w) \wedge (\neg(\mathbf{O}(x))))))))$
prod-cons	0 1 2 3	$\neg(((\mathbf{G}(\neg(p))) \wedge (\mathbf{G}(\mathbf{F}((q) \wedge ((q) \mathbf{S}(r)))))) \wedge (\mathbf{G}(\mathbf{F}(((q) \wedge ((q) \mathbf{S}(r)) \rightarrow ((s) \mathbf{S}(t)))))))$ $\neg((\mathbf{G}((p) \rightarrow ((p) \mathbf{S}((q) \mathbf{S}((r) \mathbf{S}((s) \mathbf{S}(t))))))) \wedge (\mathbf{G}(\mathbf{F}(p))))$ $\mathbf{G}((p) \rightarrow (\mathbf{F}(((q) \wedge (r)) \wedge (s))))$ $\mathbf{G}((p) \rightarrow (\mathbf{F}(q)))$
production -cell	0 1	$\neg(\mathbf{G}(\mathbf{F}(((p) \vee (q)) \wedge (\mathbf{O}(r) \wedge (\mathbf{O}(((s) \vee (t)) \wedge (\mathbf{O}(u) \wedge$ $(\mathbf{O}(((v) \vee (w)) \wedge (\mathbf{O}(((x) \vee (y)) \wedge (\mathbf{O}(z))))))))))))$ $\neg(\mathbf{G}(\mathbf{F}(((p) \vee (q)) \wedge (\mathbf{Y}(\mathbf{O}(r) \wedge (\mathbf{Y}(\mathbf{O}(((s) \vee (t)) \wedge (\mathbf{Y}(\mathbf{O}(u) \wedge$ $(\mathbf{Y}(\mathbf{O}(((v) \vee (w)) \wedge (\mathbf{Y}(\mathbf{O}(((x) \vee (y)) \wedge (\mathbf{Y}(\mathbf{O}(z))))))))))))))))$
bc-57 -sensors	0	$\neg(\mathbf{G}(\mathbf{F}((p) \wedge (\mathbf{O}(q) \wedge (\mathbf{F}(r) \wedge (\mathbf{O}(s)))))))$
srg5	$\neg L$ $\neg L, nv$	$\neg((((\mathbf{F}(\mathbf{G}(\neg(p)))) \wedge (\mathbf{G}(\mathbf{F}(q)))) \wedge (\mathbf{G}(\mathbf{F}(r)))) \rightarrow (\mathbf{F}((s) \mathbf{S}((t) \mathbf{S}((u) \mathbf{S}((v) \mathbf{S}(w))))))))$ $\neg((((\mathbf{F}(\mathbf{G}(\neg(p)))) \wedge (\mathbf{G}(\mathbf{F}(q)))) \wedge (\mathbf{G}(\mathbf{F}(r)))) \rightarrow (\mathbf{F}((s) \mathbf{S}((t) \mathbf{S}((u) \mathbf{S}((v) \mathbf{S}(w)))))))) \wedge$ $((\mathbf{F}(\mathbf{G}(\neg(p)))) \wedge (\mathbf{G}(\mathbf{F}(q)))) \wedge (\mathbf{G}(\mathbf{F}(r))))$

(Blue): only for preliminary experiments w/ incremental BMC.

Symbolic Loop Detection

[Schuppan, Biere '04]



$$V^L = V \cup \{u, just_i, ls, lb, lc\}$$

$$T^L = T \wedge (lb' \leftrightarrow ls \vee lb) \wedge (ls \rightarrow u' = v) \wedge (lb \rightarrow u' = u) \\ \wedge (just'_i \rightarrow (just_i \vee (ls \vee lb) \wedge just_i(v))) \\ \wedge (lc \rightarrow (lb \wedge u = v \wedge just_i))$$

$$I^L = I \wedge \neg lb \wedge \neg just_i$$

There exists a **just loop** in $K \Leftrightarrow$ there is a **reachable state with $lc = 1$** in K^L .